Annotatio et Erratum

A Physical Interpretation of the Cusp Conditions for Molecular Wave Functions

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The third term in Eq. (21), page 60, should be

$$\left(-\frac{1}{4}\Delta_0 - \sum_{\alpha} \frac{2Z_{\alpha}}{r_{0\alpha}}\right) \qquad \text{instead of} \qquad \left(-\frac{1}{2}\Delta_0 - \sum_{\alpha} \frac{Z_{\alpha}}{r_{0\alpha}}\right). \tag{1}$$

The following remark may be added.

The expansion (22) can be simplified for 2-electron systems. If S=0, the spatial wave function must be symmetric with respect to a permutation of electrons 1 and 2. This means, that the second term in (22) must vanish ($c \equiv 0$). If S=1, the spatial wave function must be antisymmetric, with the result that the first term in (22) vanishes identically $[\Psi(\mathbf{r}_0, \mathbf{r}_0, \ldots)] \equiv 0$.

Pack and Byers-Brown (Ref. [3] of my paper) state, that this alternative still obtains for n-electron systems with any n > 2. This statement needs some clarification. Only in the case of maximal spin S = n/2, where Ψ must be antisymmetric in all electrons, we can still say that the first term in Eq. (22) must always vanish identically. For S < n/2, there are f_S^n different spatial wave functions Ψ_i for the same energy, which span their reducible representation \mathfrak{D}_S^n of the permutation group. They can indeed be so chosen, that the matrix representation of the special permutation P_{12} is diagonal and has diagonal elements equal to +1 or -1. For those Ψ_i which belong to rows with -1 the first term and for those which belong to rows with +1 the second term in their expansion (22) must vanish. However, there is no longer any alternative, since both cases occur in the expression

$$\Phi_{S,M_S} = \sum_{i=1}^{f_S^n} \Psi_i \, \Theta_{S,M_S,i} \tag{2}$$

for the complete wave function of a single state including spin. Moreover, any other choice of the degenerate basis, while leaving (2) invariant, would lead to a situation, where the Ψ_i are neither symmetric nor antisymmetric with respect to interchange of electrons 1 and 2.

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